

Lie Symmetry Methods for Multidimensional Linear Parabolic PDEs and Diffusions

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Certificate of Authorship/ Originality

I certify that the work in this thesis has not previously been submitted for a degree nor has it been submitted as part of requirements for a degree except as fully acknowledged within the text. I also certify that the thesis has been written by me. Any help that I have received in my research work and the preparation of the thesis itself has been acknowledged. In addition, I certify that all information sources and literature used are indicated in the thesis.

Signature of Student

A handwritten signature in black ink, appearing to be 'D. L. ...', written in a cursive style.

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